

CONTENTS

PREFACE	i
CHAPTER I. THE REAL AND COMPLEX NUMBERS	1
THE NATURAL NUMBERS AND THE INTEGERS	
THE RATIONAL NUMBERS	
THE REAL NUMBERS	
PROPERTIES OF THE REAL NUMBERS	
INTERVALS AND APPROXIMATION	
THE GEOMETRIC PROGRESSION AND THE BINOMIAL THEOREM	
THE COMPLEX NUMBERS	
CHAPTER II. THE LIMIT OF A SEQUENCE OF NUMBERS	27
SEQUENCES AND LIMITS	
EXISTENCE OF CERTAIN FUNDAMENTAL LIMITS	
DEFINITION OF ϵ	
PROPERTIES OF CONVERGENT SEQUENCES	
SUBSEQUENCES AND CLUSTER POINTS	
A LITTLE TOPOLOGY	
INFINITE SERIES	
CHAPTER III. FUNCTIONS AND CONTINUITY	53
FUNCTIONS	
POLYNOMIAL FUNCTIONS	
CONTINUITY	
CONTINUITY AND TOPOLOGY	
DEEPER ANALYTIC PROPERTIES OF CONTINUOUS FUNCTIONS	
POWER SERIES FUNCTIONS	
THE ELEMENTARY TRANSCENDENTAL FUNCTIONS	
ANALYTIC FUNCTIONS AND TAYLOR SERIES	
UNIFORM CONVERGENCE	
CHAPTER IV. DIFFERENTIATION, LOCAL BEHAVIOR	85
THE LIMIT OF A FUNCTION	
THE DERIVATIVE OF A FUNCTION	
CONSEQUENCES OF DIFFERENTIABILITY, THE MEAN VALUE THEOREM	
THE EXPONENTIAL AND LOGARITHM FUNCTIONS	
THE TRIGONOMETRIC AND HYPERBOLIC FUNCTIONS	
L'HOPITAL'S RULE	
HIGHER ORDER DERIVATIVES	
TAYLOR POLYNOMIALS AND TAYLOR'S REMAINDER THEOREM	
THE GENERAL BINOMIAL THEOREM	
MORE ON PARTIAL DERIVATIVES	

CHAPTER V. INTEGRATION, AVERAGE BEHAVIOR	121
INTEGRALS OF STEP FUNCTIONS	
INTEGRABLE FUNCTIONS	
THE FUNDAMENTAL THEOREM OF CALCULUS	
CONSEQUENCES OF THE FUNDAMENTAL THEOREM	
AREA OF REGIONS IN THE PLANE	
EXTENDING THE DEFINITION OF INTEGRABILITY	
INTEGRATION IN THE PLANE	
CHAPTER VI. INTEGRATION OVER SMOOTH CURVES	
IN THE PLANE	161
SMOOTH CURVES IN THE PLANE	
ARC LENGTH	
INTEGRATION WITH RESPECT TO ARC LENGTH	
CONTOUR INTEGRALS	
VECTOR FIELDS, DIFFERENTIAL FORMS, AND LINE INTEGRALS	
INTEGRATION AROUND CLOSED CURVES, AND GREEN'S THEOREM	
CHAPTER VII. THE FUNDAMENTAL THEOREM OF ALGEBRA,	
AND THE FUNDAMENTAL THEOREM OF ANALYSIS..	197
CAUCHY'S THEOREM	
BASIC APPLICATIONS OF THE CAUCHY INTEGRAL FORMULA	
THE FUNDAMENTAL THEOREM OF ALGEBRA	
THE MAXIMUM MODULUS PRINCIPLE	
THE OPEN MAPPING THEOREM	
AND THE INVERSE FUNCTION THEOREM	
UNIFORM CONVERGENCE OF ANALYTIC FUNCTIONS	
ISOLATED SINGULARITIES, AND THE RESIDUE THEOREM	
APPENDIX. EXISTENCE AND UNIQUENESS	
OF A COMPLETE ORDERED FIELD	223