

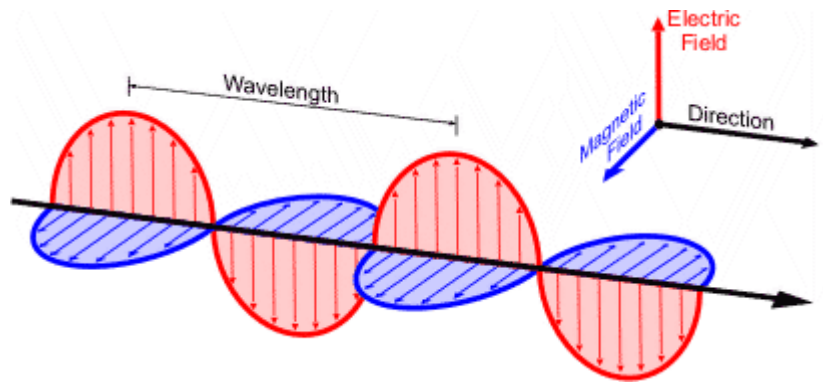
# EM waves and refraction

# Homeworks

- HW 1 will be posted today, (9/1/2017)
- HW 1 will be due next Fri (9/8/2017)
  - Analytic problems must be turned in at class (or before)
  - Matlab scripts must be emailed to [Quant.Optics@Colorado.edu](mailto:Quant.Optics@Colorado.edu) before 11:30
- Office hours are:
  - Mon 1-2 PM
  - Thur 10-11 AM
  - JSCBB 3<sup>rd</sup> floor, A-wing common area

- Last class
  - What is light
  - Detection of light
  - Properties of EM waves
- This class
  - More about waves
  - Refraction
  - Lenses

# Properties of light – propagating EM wave



## Waveforms of Electromagnetic Radiation States

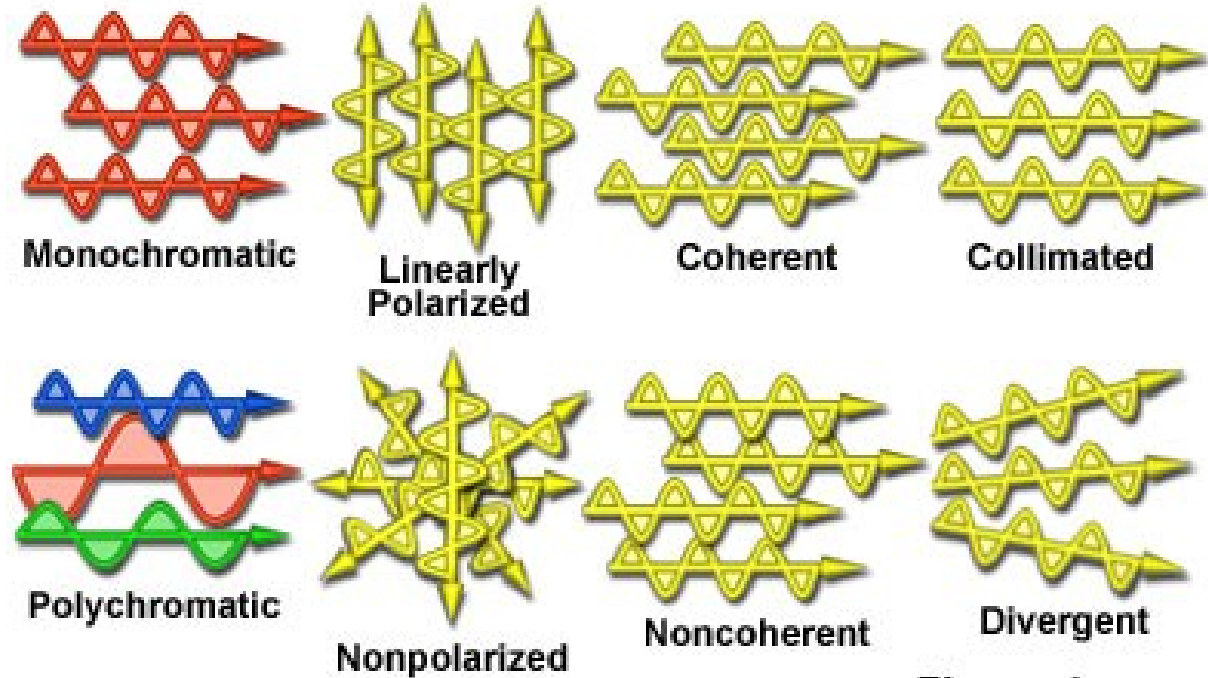
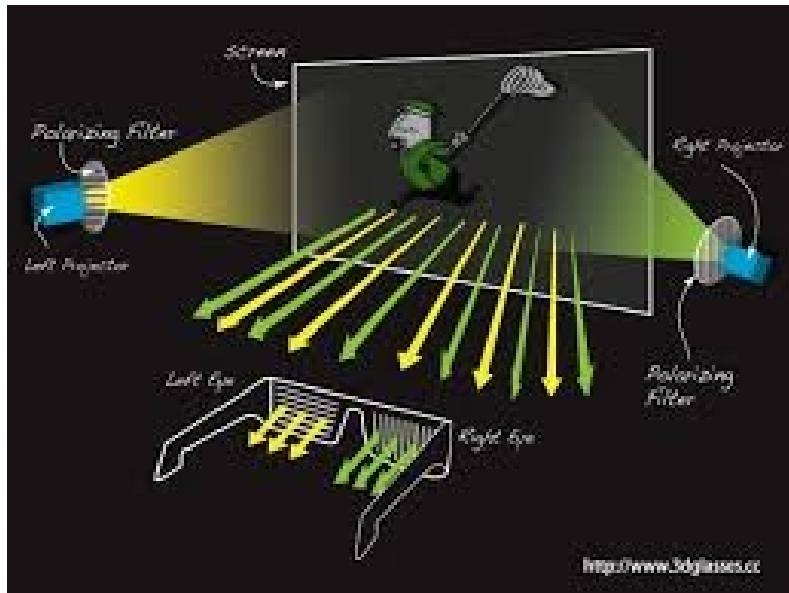


Figure 4

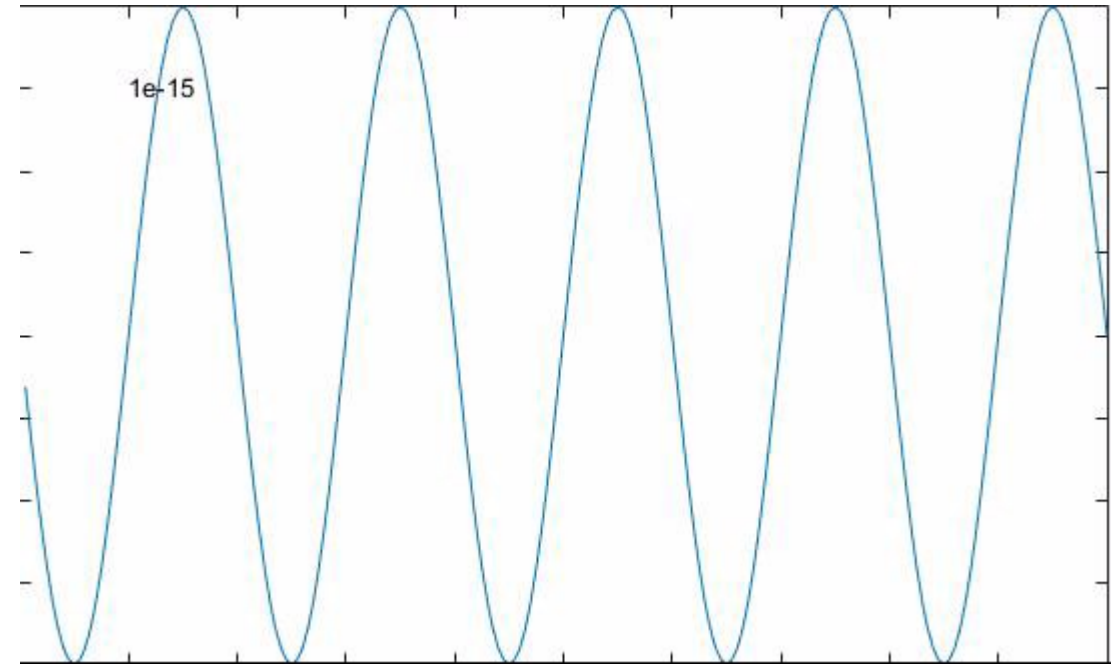
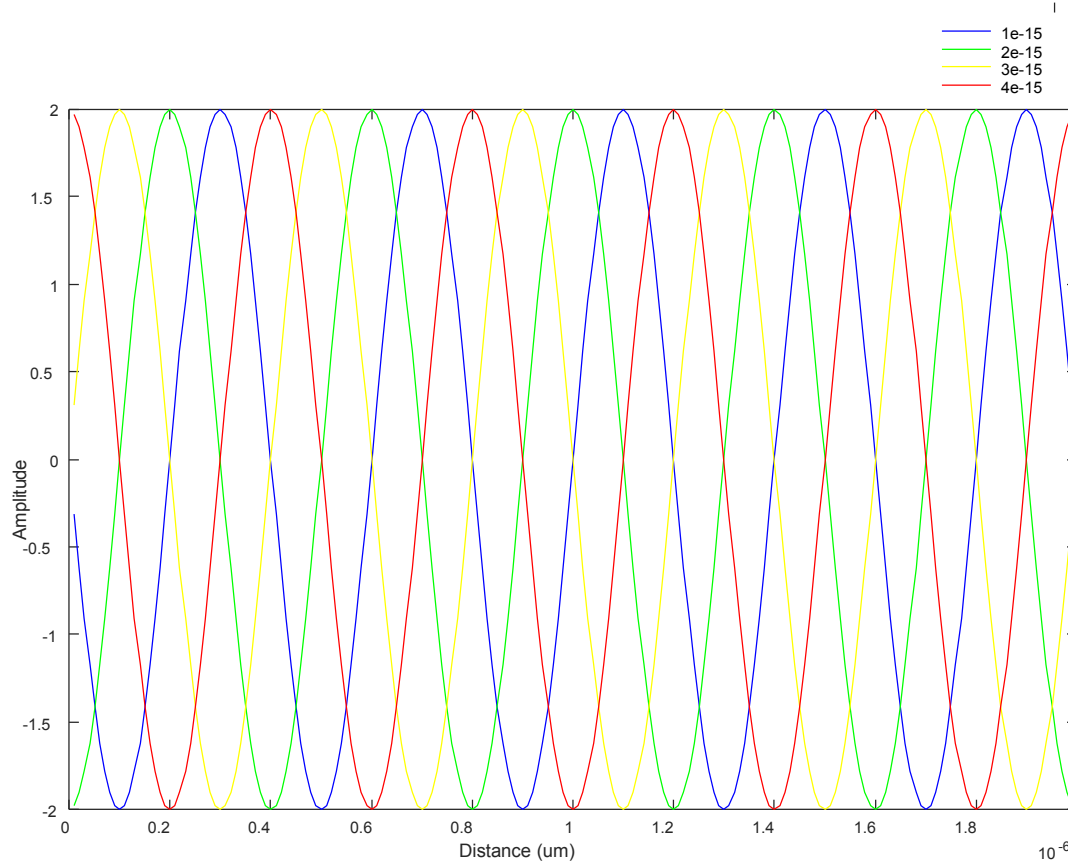


# Plane wave properties

A = amplitude  
k = wave number =  $2\pi/\lambda$   
 $\omega$  = frequency =  $2\pi f$

$$y(x, t) = A \cos(kx - \omega t + \varphi)$$

Vary t

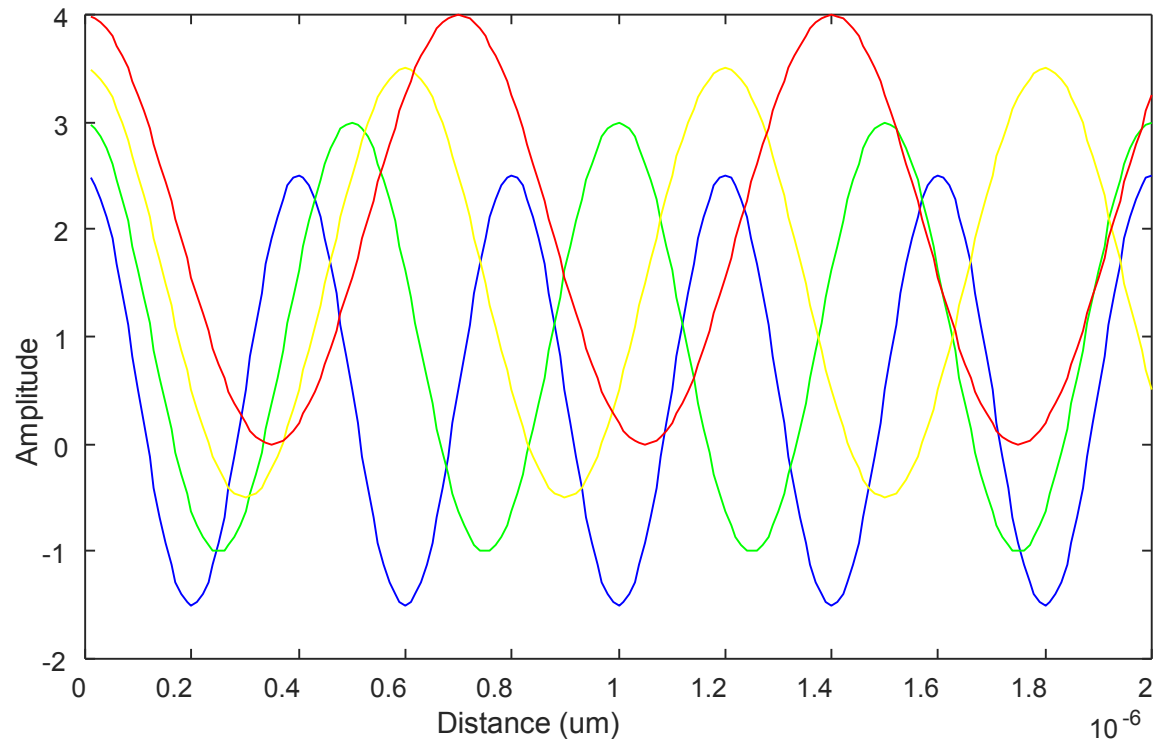


# Plane wave properties

$$y(x, t) = A \cos(kx - \omega t + \varphi)$$

- 400 nm
- 500 nm
- 600 nm
- 700 nm

Vary  $\lambda$

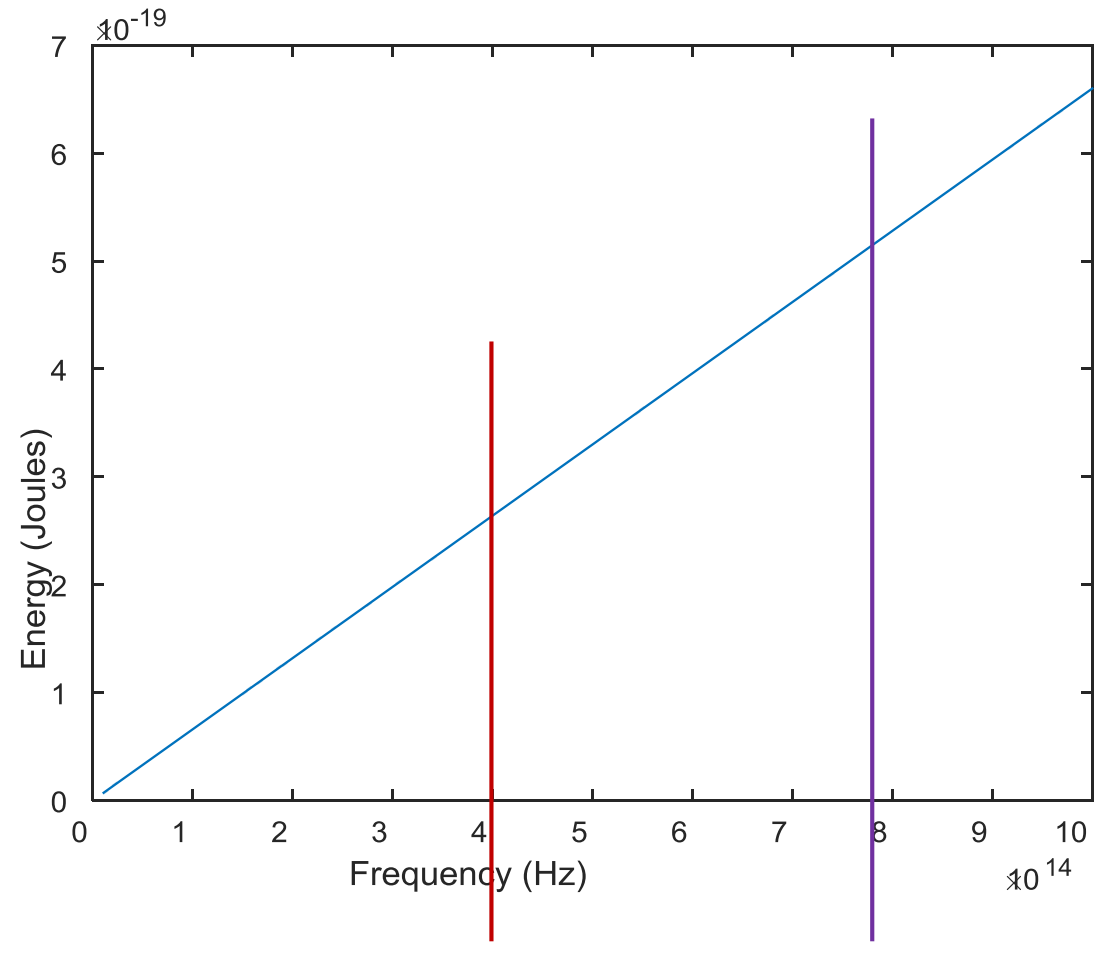
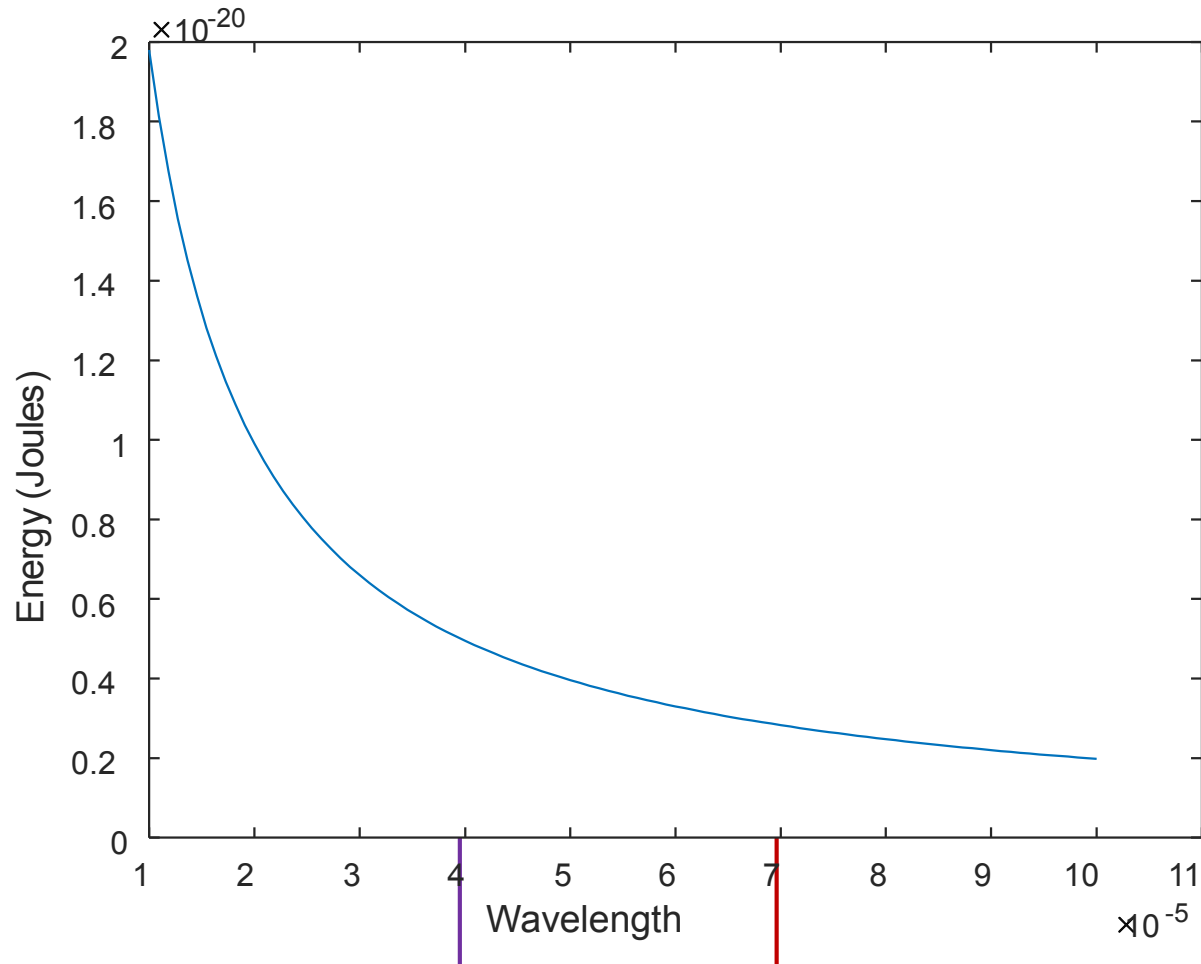


# Energy of light

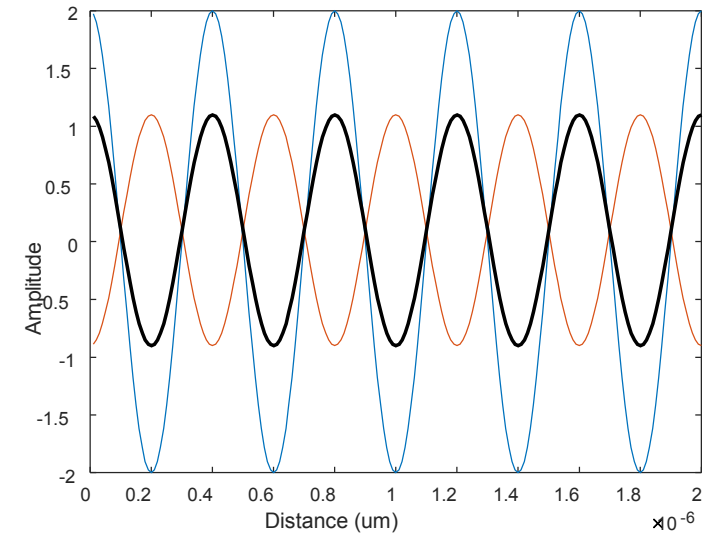
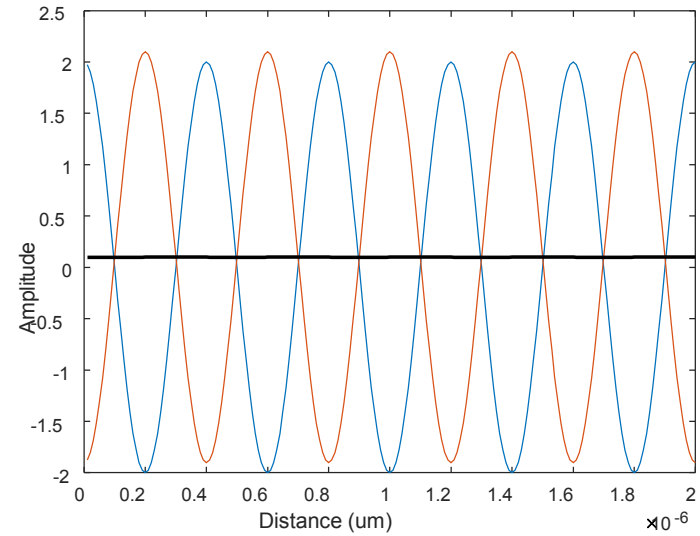
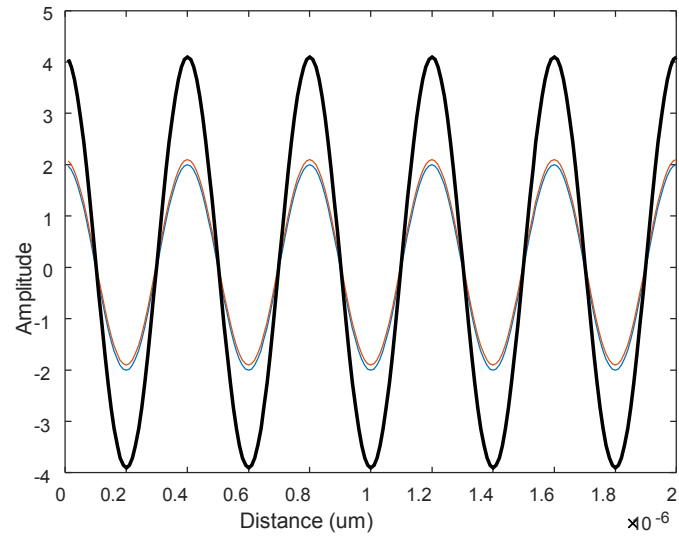
$$E = hf$$
$$= hc/\lambda$$

$$u_E = \frac{1}{2} \epsilon_0 E^2$$

$$u_B = \frac{1}{2\mu_0} B^2$$



# Wave Interference

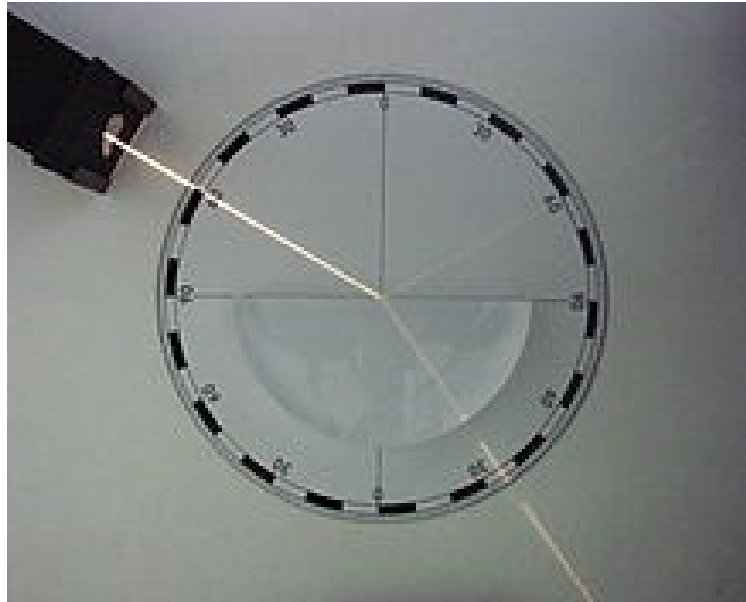
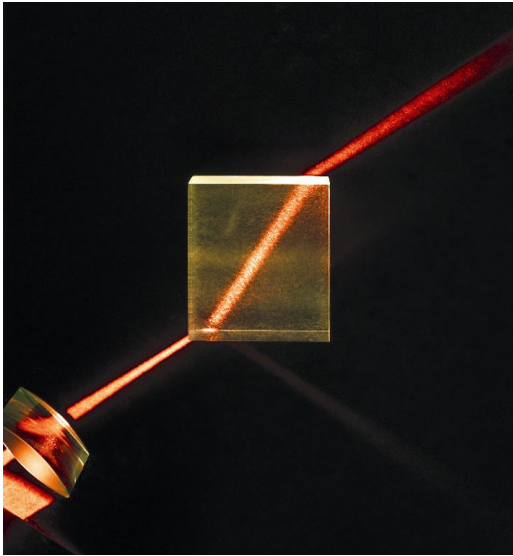




# Refraction

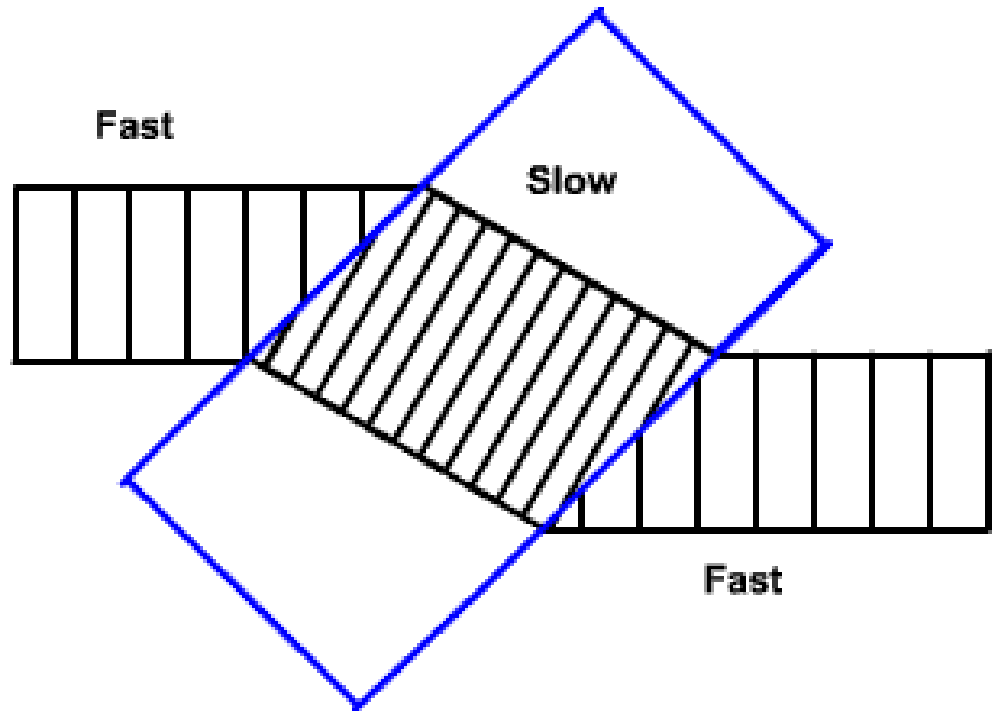
<http://hyperphysics.phy-astr.gsu.edu/hbase/geoopt/refr.html>

- Wave propagates between 2 different media
- Conservation of momentum and conservation of energy
- Amount light slowed is referred to as index of refraction ( $n$ )



# Snell's law

Velocity is slowed in new medium

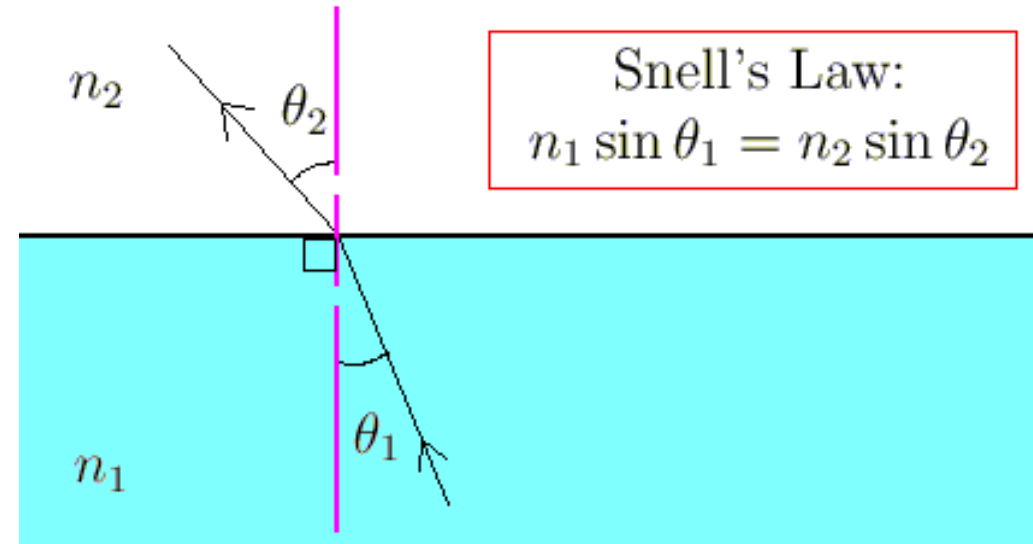


$$v = c/n$$

$$v = v/\lambda$$

$$\lambda = c/vn$$

$$\lambda = \lambda_o/n$$

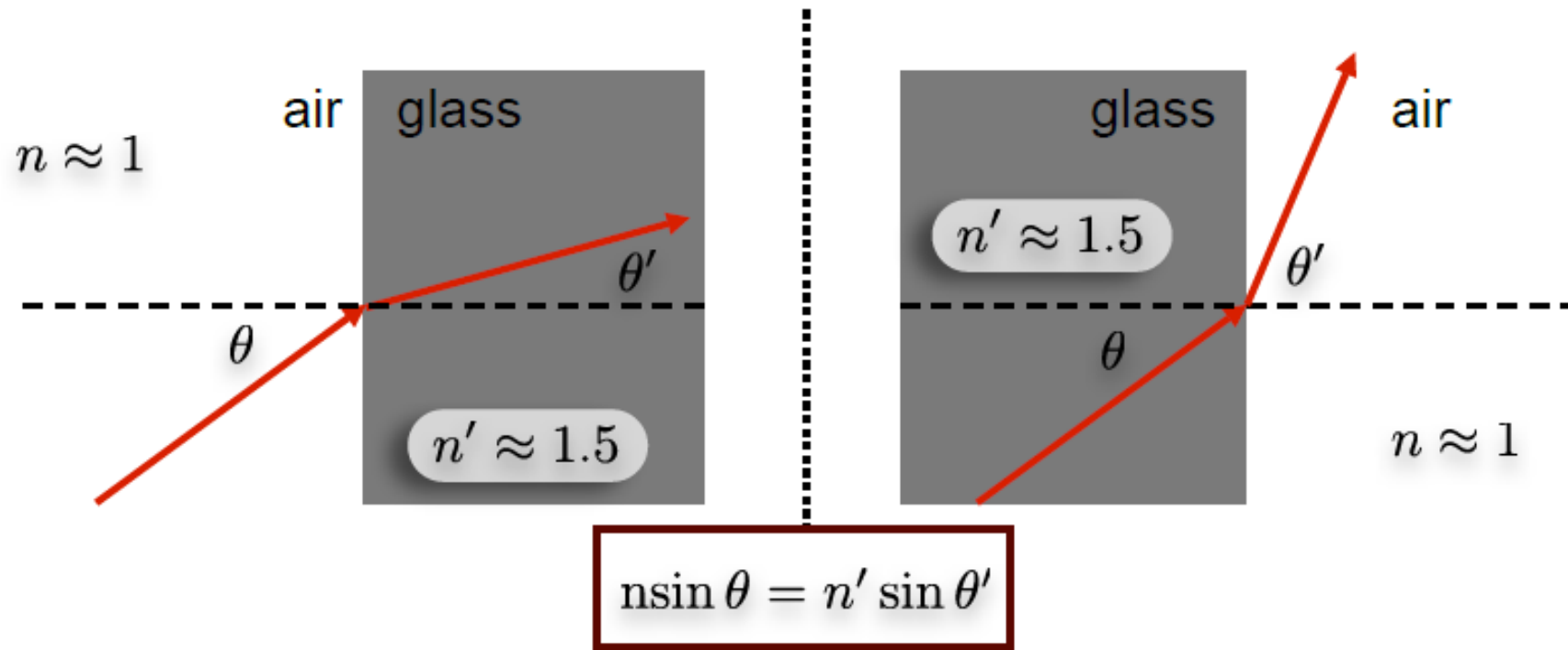


Vacuum	1
Air	1.000293
Helium	1.000036

32  
5

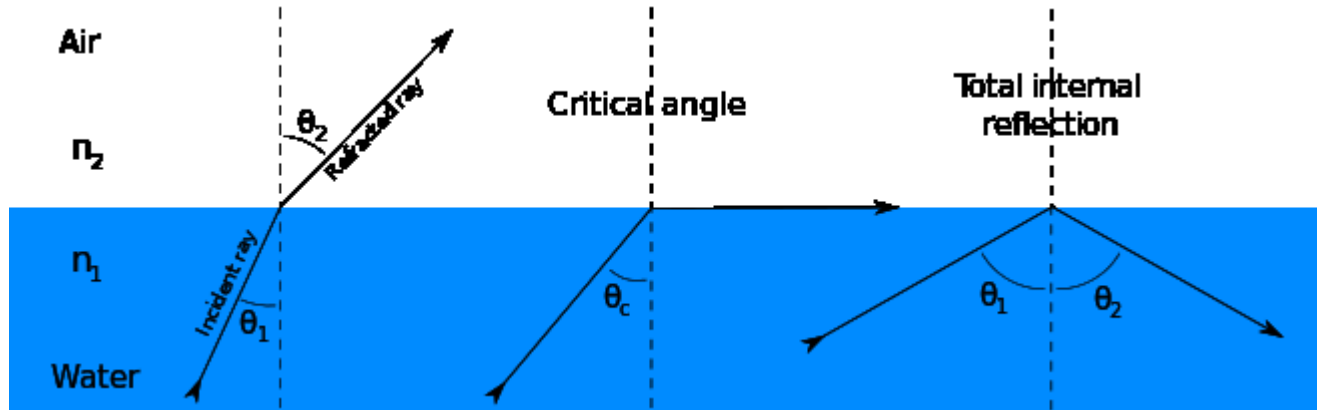
Crown glass	1.52
Flint glass (typical)	1.62
Cubic zirconia	2.15
Diamond	2.42

Back and forth...



# Total internal reflection

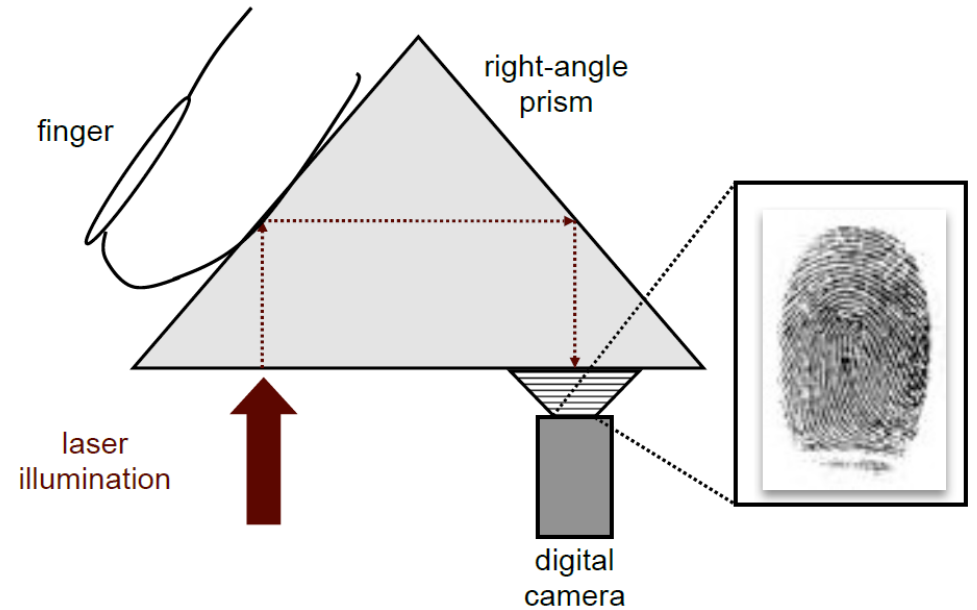
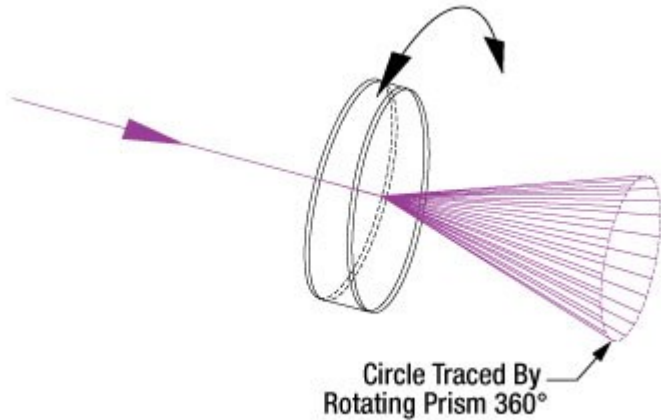
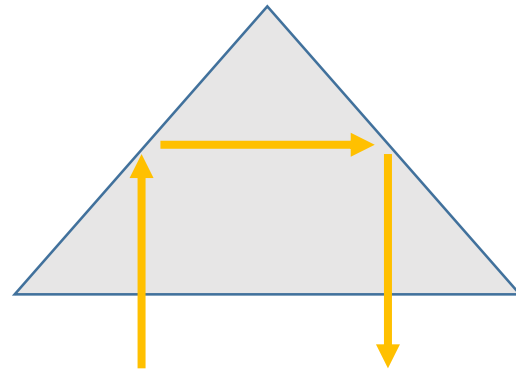
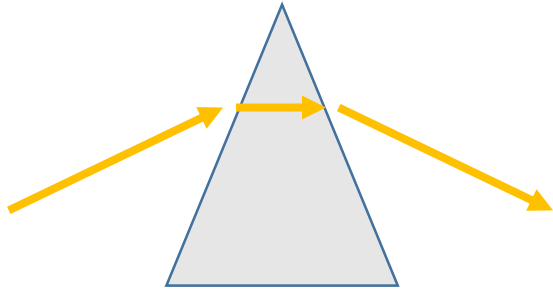
- Consider moving from dense to less dense material



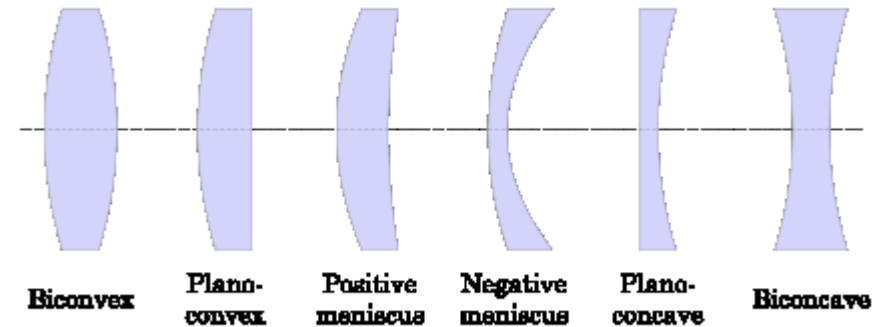
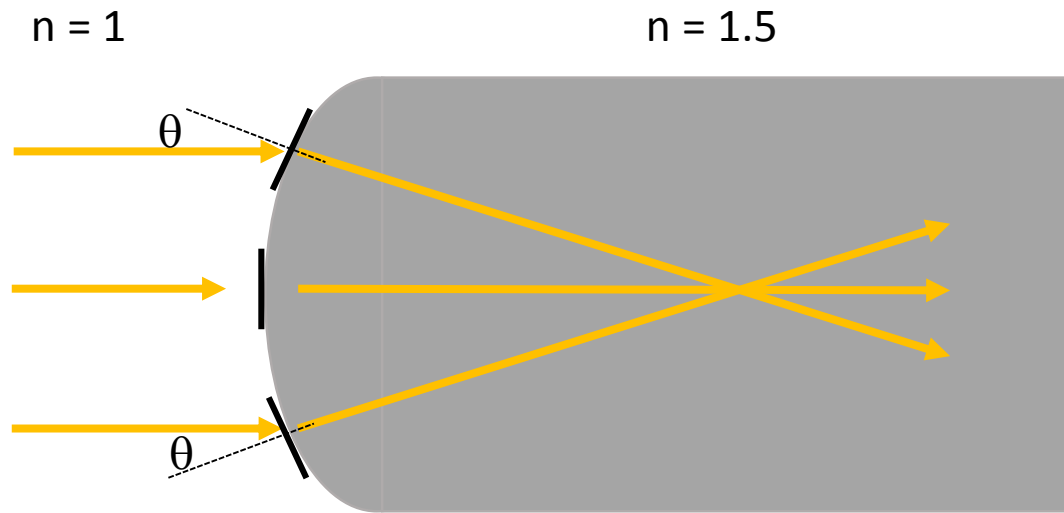
At critical angle, an evanescent wave exists but rapidly decays

# What can you do with refraction?

- Prisms:



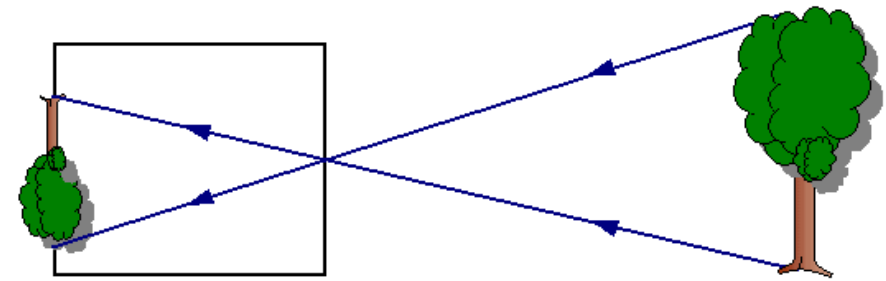
# Incident light on a curved surface (Otherwise known as a lens)



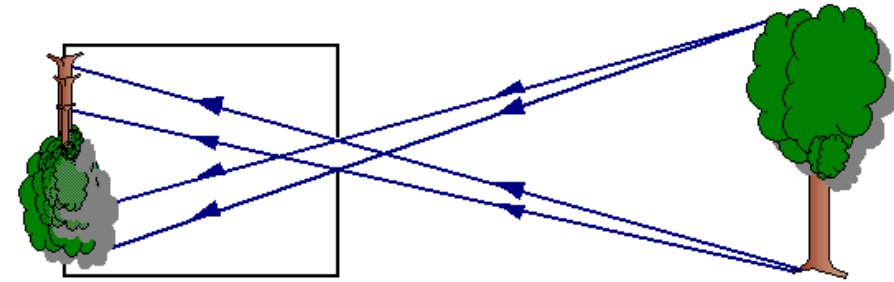
Spherical lenses are the easiest to make – grind with a lathe

# Lenses vs pinhole

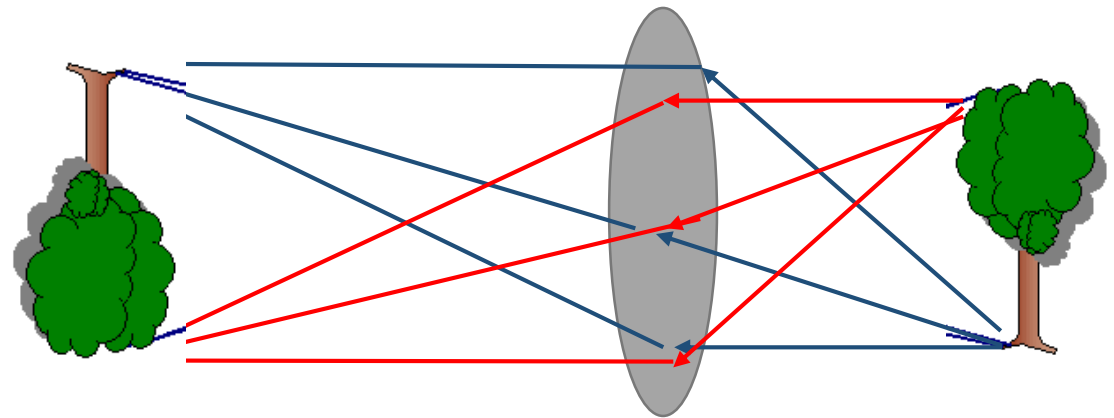
- With pinhole cameras, there was always a trade off between sharpness and brightness set by the size of the aperture
- What we want is to collect all the rays emanating from a single spot, and put them all on the same place
- Have to change the light somehow, since light (in the absence of matter) travels in a straight line
- Lenses enable us both bright and sharp images



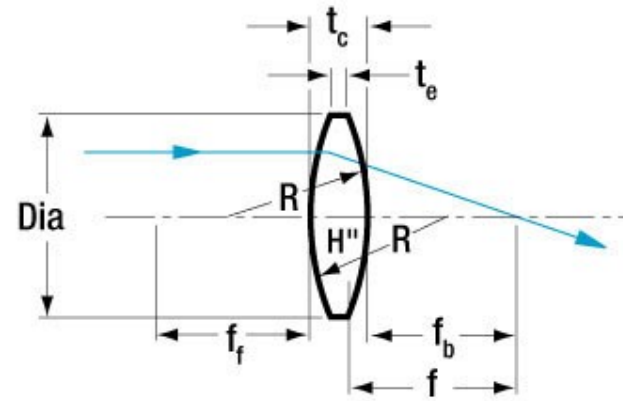
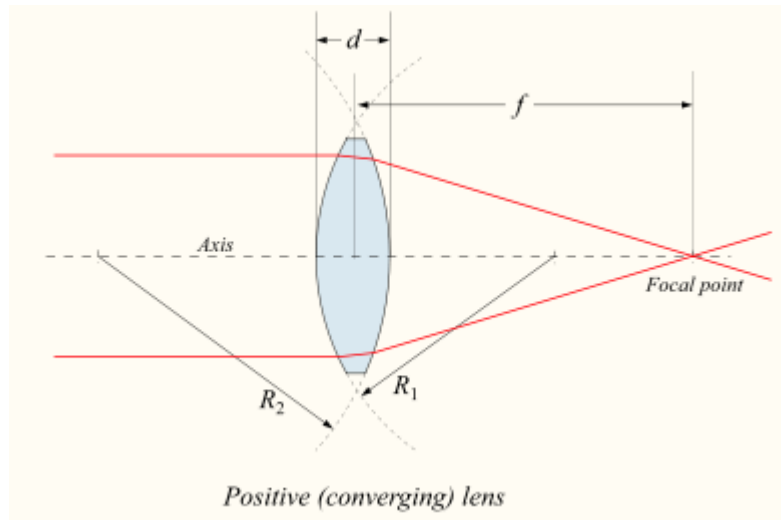
Clear upside down (inverted) image with a small pinhole



Fuzzy out of focus image with a large pinhole

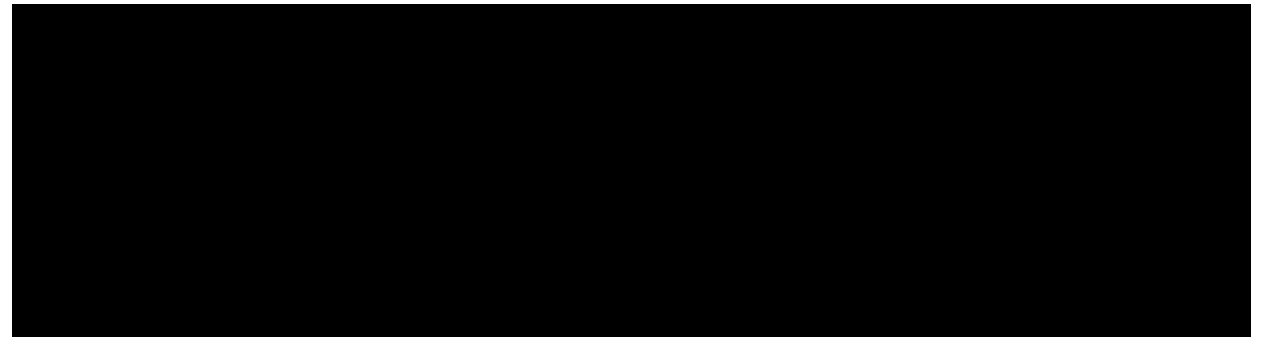


# Lens makers equation



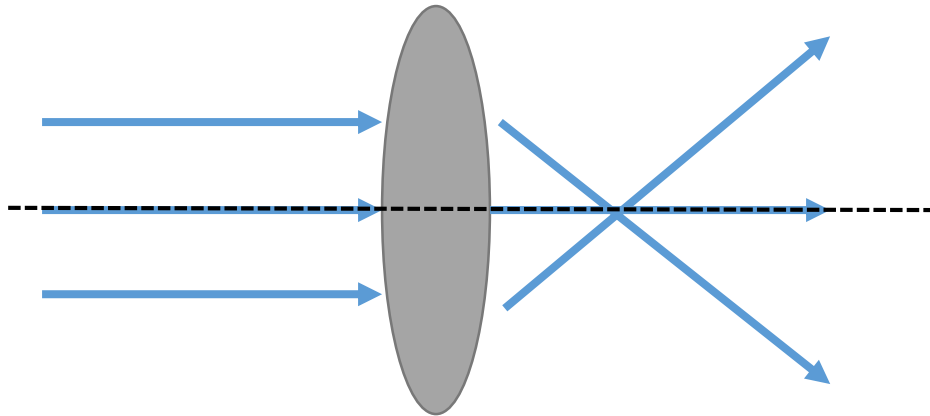
- $f$ : Focal Length
- $f_b$ : Back Focal Length
- $f_f$ : Front Focal Length
- $R$ : Radius of Curvature
- $t_c$ : Center Thickness
- $t_e$ : Edge Thickness
- $H''$ : Back Principal Plane
- Dia: Diameter

$$\frac{1}{f} = (n - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} + \frac{(n - 1)d}{nR_1R_2} \right],$$

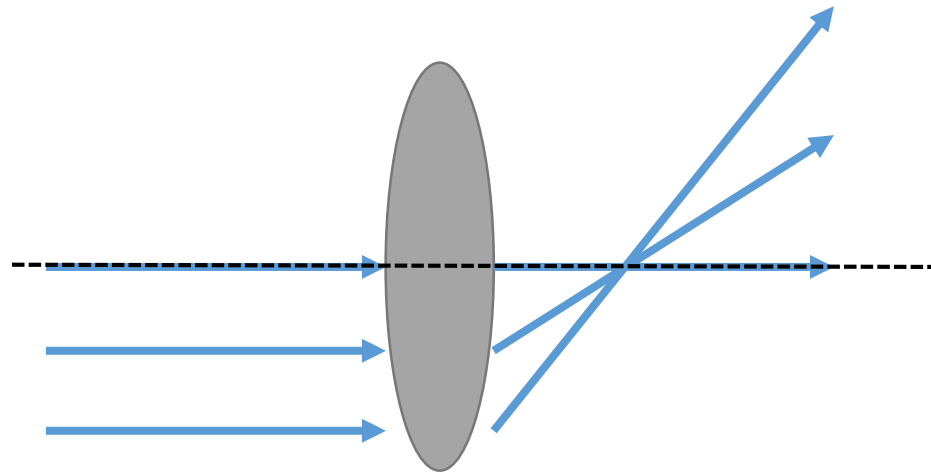
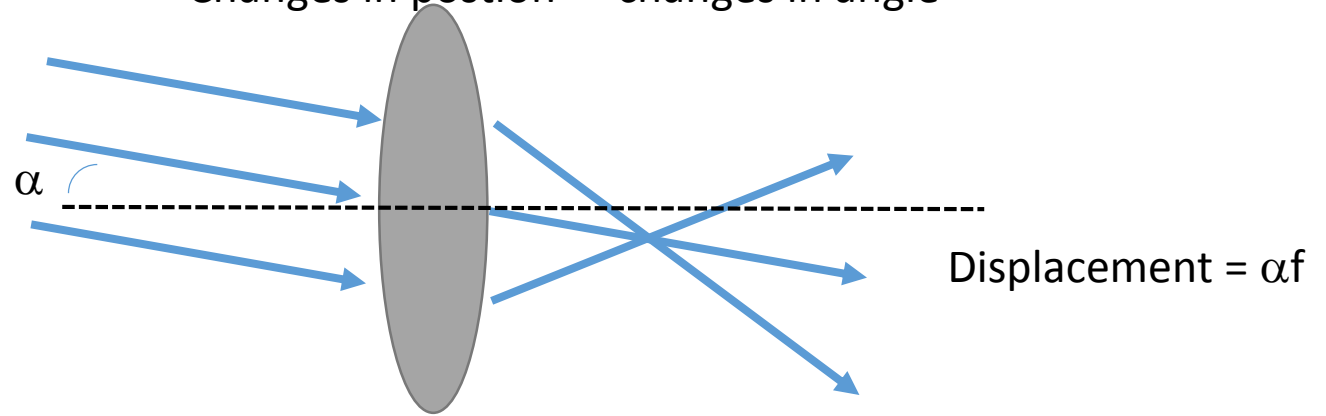




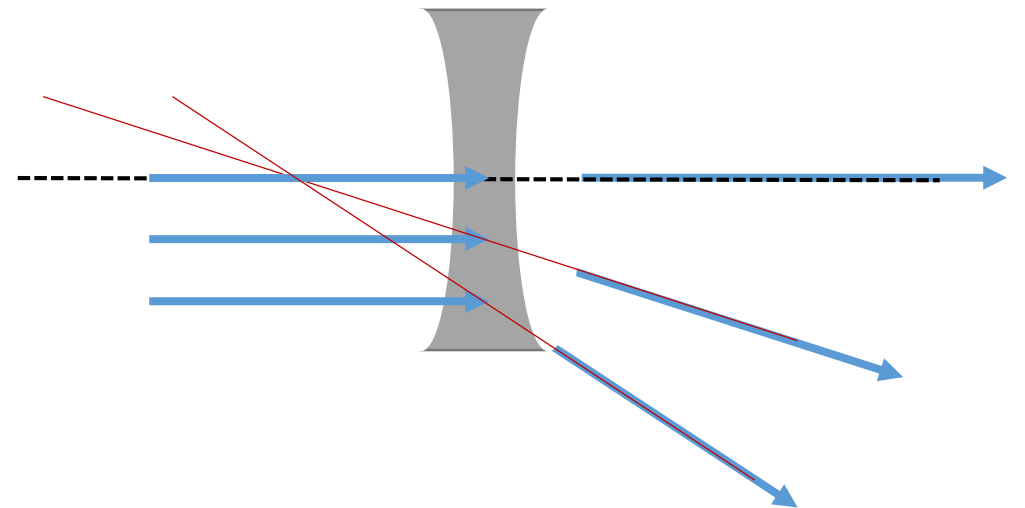
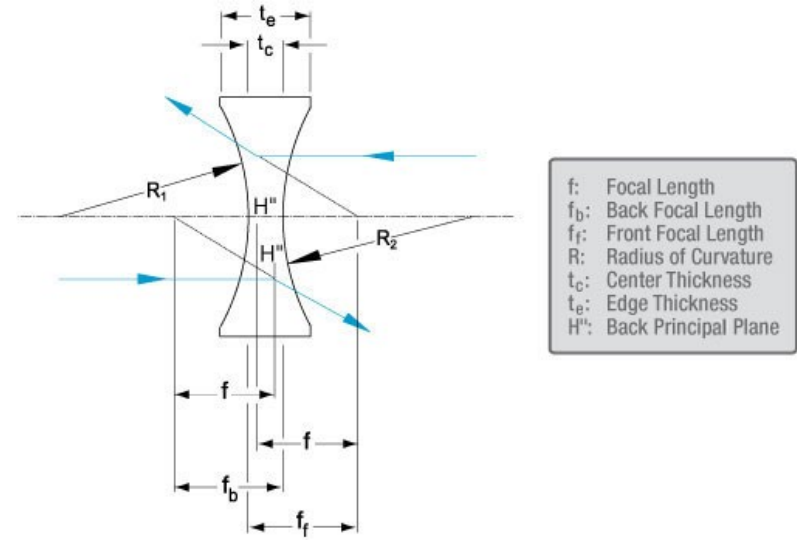
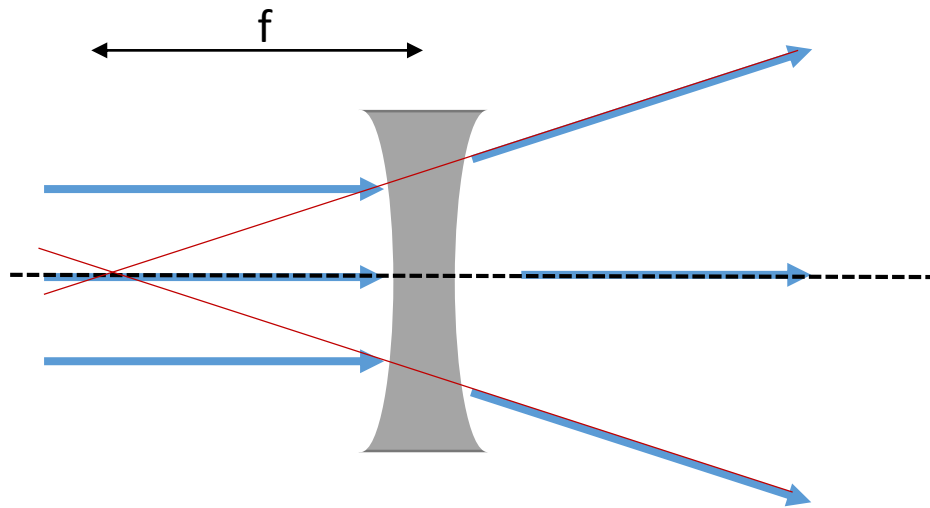
# Ray optics – convex lens



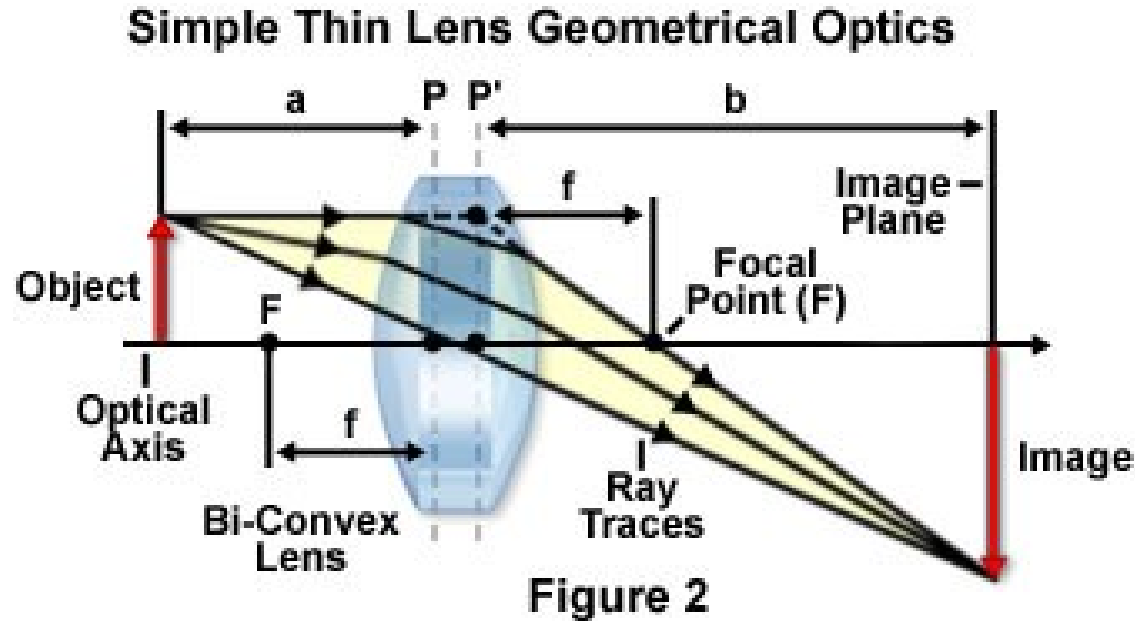
Changes in angle  $\rightarrow$  changes in position  
Changes in position  $\rightarrow$  changes in angle



# Ray optics – concave lens



# Ray optics rules

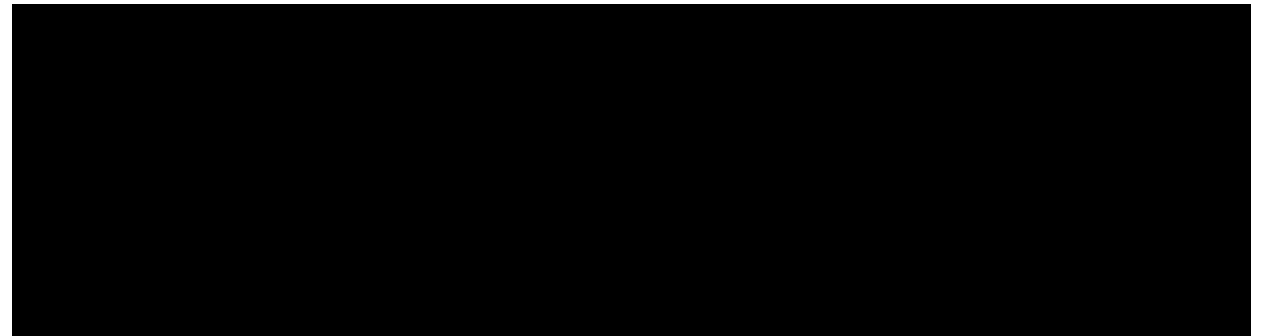


1. Draw a line to the center of the lens, it continues
2. Draw a line perpendicular to the lens axis, it goes through the focal point
3. Draw a line through the focal point, it goes straight

Light is reversible (time invariant)

If it's before the focal plane, draw as if it came from the focal point, forms a virtual image

$$\frac{1}{f} = (n - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} + \frac{(n - 1)d}{nR_1R_2} \right],$$



On to Matlab...