

\$TITLE Model M6-2: 2x2 (two goods, two factors) benchmark taxes  
 \* Positive tax in the X sector in the benchmark

\$ONTEXT

|                | <i>Production Sectors</i> |          |          | <i>Consumers</i> |   |             |
|----------------|---------------------------|----------|----------|------------------|---|-------------|
| <i>Markets</i> | /                         | <i>X</i> | <i>Y</i> | <i>W</i>         | / | <i>CONS</i> |
|                |                           |          |          |                  |   |             |
| <i>PX</i>      | /                         | 100      |          | -100             | / |             |
| <i>PY</i>      | /                         |          | 100      | -100             | / |             |
| <i>PW</i>      | /                         |          |          | 200              | / | -200        |
| <i>PL</i>      | /                         | -20      | -60      |                  | / | 80          |
| <i>PK</i>      | /                         | -60      | -40      |                  | / | 100         |
| <i>TAX</i>     | /                         | -20      | 0        |                  | / | 20          |
|                |                           |          |          |                  |   |             |

Assume that this is a 100% tax on labor in X:  $TLX = 1$ .  
 Let the CONSUMER price (wage) of labor equal 1:  $PL = 1$ .  
 The PRODUCER price (cost) of labor in X is equal to 2:  
 $PL * (1 + TLX) = 2$

\$OFFTEXT

**SCALAR** TX      Proportional output tax on sector X,  
 TY      Proportional output tax on sector Y,  
 TLX      Ad-valorem tax on labor inputs to X,

TKX Ad-valorem tax on capital inputs to X  
TAXREV Total tax revenue from all sources;

## POSITIVE VARIABLES

X Activity level for sector X  
Y Activity level for sector Y  
W Activity level for sector W  
PX Price index for commodity X  
PY Price index for commodity Y  
PL Price index for primary factor L  
PK Price index for primary factor K  
PW Price index for welfare (expenditure function)  
CONS Income definition for CONS  
PPLX Producer price for L in X  
PPKX Producer price for K in X  
PPX Producer price for X  
PPY Producer price for Y;

## EQUATIONS

PRF\_X Zero profit for sector X  
PRF\_Y Zero profit for sector Y  
PRF\_W Zero profit for sector W  
  
MKT\_X Supply-demand balance for commodity X

MKT\_Y      Supply-demand balance for commodity Y  
 MKT\_L      Supply-demand balance for primary factor L  
 MKT\_K      Supply-demand balance for primary factor L  
 MKT\_W      Supply-demand balance for aggregate demand  
  
 I\_CONS     Income definition for CONS  
  
 RPPLX     Relation between consumer and producer price L in X  
 RPPKX     Relation between consumer and producer price K in X  
 RPPX      Relationship between producer and consumer price of X  
 RPPY      Relationship between producer and consumer price of Y;

\*      *Zero profit conditions:*

PRF\_X..     $100 * (PPLX/2)**0.4 * (PPKX)**0.6 =G= 100 * PPX;$

PRF\_Y..     $100 * PL**0.6 * PK**0.4 =G= 100 * PPY;$

PRF\_W..     $200 * PX**0.5 * PY**0.5 =G= 200 * PW;$

\*      *Market clearing conditions:*

MKT\_X..     $100 * X =G= 100 * W * PW / PX;$

MKT\_Y..     $100 * Y =G= 100 * W * PW / PY;$

MKT\_W.. 200\*W =G= CONS/PW;

MKT\_L.. 80 =G= 20\*X\*PPX/(PPLX/2) + 60\*Y\*PPY/PL;

MKT\_K.. 100 =G= 60\*X\*PPX/PPKX + 40\*Y\*PPY/PK;

\* *Income constraints:*

I\_CONS.. CONS =E= 80\*PL + 100\*PK + 100\*PX\*X\*TX + 100\*PY\*Y\*TY +  
 TLX\*PL\*20\*X\* PPX /(PPLX/2) +  
 TKX\*PK\*60\*X\* PPX /(PPKX);

RPPLX.. PPLX =E= PL\*(1+TLX);

RPPKX.. PPKX =E= PK\*(1+TKX);

RPPX.. PPX =E= PX\*(1-TX);

RPPY.. PPY =E= PY\*(1-TY);

**MODEL** BENCHTAX /PRF\_X.X, PRF\_Y.Y, PRF\_W.W,  
 MKT\_X.PX, MKT\_Y.PY, MKT\_L.PL, MKT\_K.PK,  
 MKT\_W.PW, I\_CONS.CONS,  
 RPPLX.PPLX, RPPKX.PPKX, RPPX.PPX, RPPY.PPY /;

X.L =1;

Y.L =1;

W.L =1;

```
PL.L      =1;  
PX.L      =1;  
PY.L      =1;  
PK.L      =1;  
PW.FX     =1;  
PPLX.L    = 2;  
PPKX.L    = 1;  
PPX.L     = 1;  
PPY.L     = 1;
```

```
CONS.L    =200;
```

```
TX        =0;  
TY        =0;  
TLX       =1;  
TKX       =0;
```

```
BENCHTAX.ITERLIM = 0;  
SOLVE BENCHTAX USING MCP;
```

```
BENCHTAX.ITERLIM = 1000;  
SOLVE BENCHTAX USING MCP;
```

```
TAXREV = 100*PX.L*X.L*TX + 100*PY.L*Y.L*TY +  
          TLX*PL.L*20*X.L* PPX.L / (PPLX.L/2) +  
          TKX*PK.L*60*X.L* PPX.L / (PPKX.L);
```

**DISPLAY** TAXREV;

\* *In the first counterfactual, we replace the tax on*  
 \* *labor inputs by a uniform tax on both factors:*

TLX = 0.25;  
 TKX = 0.25;  
 TX = 0;  
 TY = 0;

**SOLVE** BENCHTAX USING MCP;

$$\begin{aligned} \text{TAXREV} = & 100 * \text{PX.L} * \text{X.L} * \text{TX} + 100 * \text{PY.L} * \text{Y.L} * \text{TY} + \\ & \text{TLX} * \text{PL.L} * 20 * \text{X.L} * \text{PPX.L} / (\text{PPLX.L} / 2) + \\ & \text{TKX} * \text{PK.L} * 60 * \text{X.L} * \text{PPX.L} / (\text{PPKX.L}); \end{aligned}$$

**DISPLAY** TAXREV;

\* *Now demonstrate that a 25% tax on all inputs*  
 \* *is equivalent to a*  
 \* *20% tax on the output (or all outputs if more than one)*

TLX = 0;  
 TKX = 0;  
 TX = 0.2;  
 TY = 0;

**SOLVE** BENCHTAX USING MCP;

$$\begin{aligned} \text{TAXREV} = & 100 * \text{PX.L} * \text{X.L} * \text{TX} + 100 * \text{PY.L} * \text{Y.L} * \text{TY} + \\ & \text{TLX} * \text{PL.L} * 20 * \text{X.L} * \text{PPX.L} / (\text{PPLX.L} / 2) + \\ & \text{TKX} * \text{PK.L} * 60 * \text{X.L} * \text{PPX.L} / (\text{PPKX.L}); \end{aligned}$$

**DISPLAY** TAXREV;

- \* *Demonstrate that a 20% tax on the X sector output is*
- \* *equivalent to a 25% subsidy on Y sector output*
- \* *(assumes that the funds for the subsidy can be raised*
- \* *lump sum from the consumer!)*

$$\text{TKX} = 0;$$

$$\text{TLX} = 0;$$

$$\text{TX} = 0;$$

$$\text{TY} = -0.25;$$

**SOLVE** BENCHTAX USING MCP;

$$\begin{aligned} \text{TAXREV} = & 100 * \text{PX.L} * \text{X.L} * \text{TX} + 100 * \text{PY.L} * \text{Y.L} * \text{TY} + \\ & \text{TLX} * \text{PL.L} * 20 * \text{X.L} * \text{PPX.L} / (\text{PPLX.L} / 2) + \\ & \text{TKX} * \text{PK.L} * 60 * \text{X.L} * \text{PPX.L} / (\text{PPKX.L}); \end{aligned}$$

**DISPLAY** TAXREV;

- \* *Show welfare under non-distortionary taxation*

$$\text{TX} = 0.20;$$

TY = 0.20;

**SOLVE** BENCHTAX USING MCP;

TAXREV = 100\*PX.L\*X.L\*TX + 100\*PY.L\*Y.L\*TY +  
          TLX\*PL.L\*20\*X.L\* PPX.L / (PPLX.L/2) +  
          TKX\*PK.L\*60\*X.L\* PPX.L / (PPKX.L);

**DISPLAY** TAXREV;

TX = 0.0;

TY = 0.0;

**SOLVE** BENCHTAX USING MCP;

TAXREV = 100\*PX.L\*X.L\*TX + 100\*PY.L\*Y.L\*TY +  
          TLX\*PL.L\*20\*X.L\* PPX.L / (PPLX.L/2) +  
          TKX\*PK.L\*60\*X.L\* PPX.L / (PPKX.L);

**DISPLAY** TAXREV;