\$TITLE: M7-2.GMS: Monopoly with fixed costs
\$ONTEXT

|  |  | Production Sectors |  |  | Consumers |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Markets | C | FC | $Y$ | W | CONS | ENTR |
| $P X$ | 100 |  |  | -100 |  |  |
| PY |  |  | 100 | -100 |  |  |
| PFC |  | 20 |  |  |  | -20 |
| PW |  |  |  | 200 | -200 |  |
| PL | -80 | -20 | -100 |  | 200 |  |
| MK | -20 |  |  |  |  | 20 |

## \$OFFTEXT

PARAMETERS

SIGMA
FC
ENDOWL
INCOMEM
INCOMEC
MODELSTAT

SIGMA: elasticity of substitution among varieties parameter setting the level of fixed costs endowment of MKT_Lor monopoly profit share (markup revenues - fixed costs) income share of the "the people" or MKT_Lor income statistic indicating model solved: $0=$ solved;

SIGMA = 9;
FC = 20;
ENDOWL = 200;

## POSITIVE VARIABLES

$X \quad$ Activity level for $X$ (output per firm)
$Y \quad$ Activity level of $Y$ output
W Activity level for welfare

PX Price of an individual X variety
PY Price of Y
PW Price index for utility (consumer price index)
PL Price of MKT_Lor

CONS Income of the representative consumer
SHAREX Share of $X$ in consumption (value share)
MARKUP Markup;

## EQUATIONS

```
PRICEX MR = MC in X (associated with X output per firm)
PRICEY Zero profit condition for Y (PY = MC)
PRICEW Zero profit condition for W (PW = MC of utility)
MKT_X Supply-demand balance for X (individual variety)
MKT_Y Supply-demand balance for Y
MKT_W Supply-demand balance for utility W (welfare)
```

```
    MKT_L Supply-demand balance for MKT_Lor
    INCOME National income
SHX Share of X in expenditure
MK Markup equation;
PRICEX.. 80*PL =G= 100*PX*(1-MARKUP);
PRICEY.. 100*PL =G= 100*PY;
PRICEW.. (0.5*PX**(1-SIGMA) + 0.5*PY**(1-SIGMA))**(1/(1-SIGMA))
        =G= PW;
MKT_X.. X*100 =G= PX**(-SIGMA)*(PW**(SIGMA-1))*CONS/2;
MKT_Y.. Y*100 =G= PY**(-SIGMA)*(PW**(SIGMA-1))*CONS/2;
MKT_W.. 200*W =G= CONS/PW;
MKT_L.. ENDOWL =E= Y*100 + X*80 + FC;
INCOME.. CONS =E= PL*ENDOWL + (100*PX*X*MARKUP - PL*FC);
SHX.. SHAREX =E= 100*PX*X / (100*PX*X + 100*PY*Y) ;
MK.. MARKUP =E= 1/(SIGMA - (SIGMA-1)*SHAREX);
```

```
MODEL MONOPOLY /PRICEX.X, PRICEY.Y, PRICEW.W,
    MKT_X.PX, MKT_Y.PY, MKT_W.PW, MKT_L.PL,
    INCOME.CONS, SHX.SHAREX, MK.MARKUP/;
```

OPTION MCP=PATH;

* set benchmark values:
X.L = 1;
Y.L = 1;
W.L = 1;
PX.L = 1;
PY.L = 1;
PL.L = 1;
PW.L = 1;
CONS.L = 200;
SHAREX.L = 0.5;
MARKUP.L = 0.20;
* choose the price of good $Y$ as numeraire
PY.FX = 1;
* check for calibration and starting-value errors
MONOPOLY.ITERLIM = 0;

SOLVE MONOPOLY USING MCP;
MONOPOLY.ITERLIM = 1000; SOLVE MONOPOLY USING MCP;

MODELSTAT = MONOPOLY.MODELSTAT - 1.; DISPLAY MODELSTAT;

```
INCOMEM = (MARKUP.L*PX.L*X.L*100 - PL.L*FC)/CONS.L;
```

INCOMEC = (PL.L*ENDOWL)/CONS.L;

DISPLAY INCOMEM, INCOMEC;

* Counterfactual: contract the size of the economy

ENDOWL = 100;
SOLVE MONOPOLY USING MCP;
INCOMEM = (MARKUP.L*PX.L*X.L*100 - PL.L*FC)/CONS.L; INCOMEC = (PL.L*ENDOWL)/CONS.L;

DISPLAY INCOMEM, INCOMEC;

* Counterfactual: expand the size of the economy

ENDOWL = 400;
SOLVE MONOPOLY USING MCP;
INCOMEM $=($ MARKUP.L*PX.L*X.L*100 - PL.L*FC)/CONS.L;
INCOMEC $=(P L . L * E N D O W L) / C O N S . L ;$
DISPLAY INCOMEM, INCOMEC;

