\$TITLE: M6-7.GMS: two households with different preferences, endowments

\$ONTEXT

adaptation of model M3-7: distortionary tax can be used for redistribution modeled as an MPEC: find the optimal tax maximizing social welfare two add-ons

- (1) allows the redistributive shares of tax revenue to be endogenous
- (2) allows an optimal lump-sum redistribution for comparison

Two household: differ in preferences and in endowments

Household A: well endowed with labor,

preference for labor-int good Y

Household B: well endowed with capital,

preference for capital-int good X

		Production Sectors					Consumers	
Markets		X	Y	WA 	WB		A	B
PX	/	100		-40	-60	/		
PY	/		100	-60	-40			
PWA	/			100			-100	
PWB	/				100			-100
PL	/	-25	-75				90	10
PK		-75	-25				10	90

The tax redistribution or sharing rule can also be interpreted as the relative number of households in each group, with all households getting an equal share of tax receipts \$OFFTEXT

PARAMETERS

```
WEIGHTA weight of consumer A in social welfare WEIGHTB weight of consumer B in social welfere;
```

```
WEIGHTA = 0.5;
WEIGHTB = 0.5;
```

VARIABLES

WS:	social wellare
TAX	endogenous tax rate on X
LS	<pre>lump sum redistibution;</pre>

NONNEGATIVE VARIABLES

```
X Activity level for sector X,
Y Activity level for sector Y,
WA Activity level for weflare for consumer A
WB Activity level for welfare for consumer B
PX Price index for commodity X,
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```
Price index for commodity Y,
PY
PΚ
        Price index for primary factor K,
        Price index for primary factor L.
PI_1
        Price index for welfare A(expenditure function),
PWA
PWB
        Price index for welfare B(expenditure function),
CONSA
        Income definition for CONSA,
CONSB
        Income definition for CONSB
        share of tax redistributed to consumer A
SHA
        share of tax redistributed to consumer B;
SHB
```

EQUATIONS

```
Social welfare function
OBJ
PRF X Zero profit for sector X
PRF Y Zero profit for sector Y
PRF WA Zero profit for sector WA (Hicksian welfare index)
       Zero profit for sector WB (Hicksian welfare index)
PRF WB
       Supply-demand balance for commodity X
MKT X
       Supply-demand balance for commodity Y
MKT Y
MKT L
       Supply-demand balance for primary factor L
       Supply-demand balance for primary factor K
MKT K
       Supply-demand balance for aggregate demand consumer A
MKT WA
       Supply-demand balance for aggregate demand consumer B
MKT WB
```

```
I CONSA Income definition for CONSA
       I CONSB Income definition for CONSB
       ADDUP Sum of the redistributive shares equals 1;
       Objective function (social weflare function) to be maxmized
OBJ..
       WS =E= (WA**WEIGHTA) * (WB**WEIGHTB);
       Zero profit conditions:
               100 * (PL**0.25 * PK**0.75) * (1+TAX) =E= 100 * PX;
PRF X..
               100 * (PL**0.75 * PK**0.25) =E= 100 * PY;
PRF Y..
              100 * PX**0.4 * PY**0.6 =E= 100 * PWA;
PRF WA..
PRF_WB.. 100 * PX**0.6 * PY**0.4 =E= 100 * PWB;
       Market clearing conditions:
MKT X..
               100 * X = E = 40*WA*PWA/PX + 60*WB*PWB/PX;
               100 * Y = E = 60*WA*PWA/PY + 40*WB*PWB/PY;
MKT Y..
MKT_WA.. 100 * WA = E = CONSA / PWA;
```

```
MKT WB..
               100 * WB = E = CONSB / PWB;
MKT L..
               90 + 10 = E = 25*X*(PX/(1+TAX))/PL + 75*Y*PY/PL;
MKT K..
               10 + 90 = E = 75*X*(PX/(1+TAX))/PK + 25*Y*PY/PK;
*
       Income constraints:
I CONSA.. CONSA = E = 90*PL + 10*PK + SHA*TAX*100*X*PX/(1+TAX) + LS;
I CONSB.. CONSB = E = 10*PL + 90*PK + SHB*TAX*100*X*PX/(1+TAX) - LS;
ADDUP.. SHA + SHB =E=1;
*MODEL MPEC /ALL/;
OPTION MPEC = nlpec;
MODEL MPEC /OBJ, PRF X.X, PRF Y.Y, PRF WA.WA, PRF WB.WB,
                MKT X.PX, MKT Y.PY, MKT L.PL,
                MKT K.PK, MKT WA.PWA, MKT WB.PWB,
                I CONSA.CONSA, I CONSB.CONSB, ADDUP /;
*
       Check the benchmark:
WS.L = 1;
X.L = 1;
```

```
Y.L
       =1;
WA.L = 1;
WB.L =1;
PL.L
       =1;
PX.L = 1;
PY.L =1;
PK.L = 1;
PWB.L =1;
PWA.L =1;
CONSA.L = 100;
CONSB.L = 100;
TAX.L =0.;
SHA.L =0.5;
SHB.L =0.5;
PWA.FX = 1;
SOLVE MPEC USING MPEC MAXIMIZING WS;
```

^{*} now allow weights in social welfare to differ * e.g., 70% of all households/voters are type A

```
WEIGHTA = 0.7;
WEIGHTB = 0.3;
* first, fix shares at 0.5, hold LS = 0
SHA.FX = 0.5i
SHB.FX = 0.5;
LS.FX = 0;
SOLVE MPEC USING MPEC MAXIMIZING WS;
* now free up the redistributive weights
SHA.UP = +INF;
SHB.UP = +INF;
SHA.LO = 0;
SHB.LO = 0;
SOLVE MPEC USING MPEC MAXIMIZING WS;
* now allow lump-sum transfers
LS.UP = +INF;
LS.LO = -INF;
SOLVE MPEC USING MPEC MAXIMIZING WS;
```

```
* now switch the weights to consumer B
WEIGHTA = 0.3;
WEIGHTB = 0.7;
SOLVE MPEC USING MPEC MAXIMIZING WS;
```